[2]

[5]

[2]

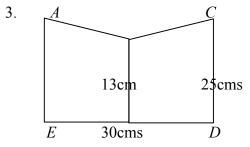
[2]

## MECHANICS (C) UNIT 2TEST PAPER 5Take $g = 9.8 \text{ ms}^{-2}$ and give all answers correct to 3 significant figures where necessary.

- A pump raises water from a reservoir at a depth of 25 m below ground level. The water is 1. delivered at ground level with speed  $12 \text{ ms}^{-1}$  through a pipe of radius 4 cm. Find
  - (i) the potential and kinetic energy given to the water each second, [4]
  - (ii) the rate, in kW, at which the pump is working.

 $[1 \text{ m}^3 \text{ of water has a mass of } 1000 \text{ kg.}]$ 

- Aliya, whose mass is m kg, is playing rounders. She rounds the first base at a speed of v ms<sup>-1</sup>, 2. making the turn on a horizontal circular path of radius r m.
  - (i) Write down, in terms of m, v and r, the magnitude of the horizontal force acting on her. [1]
  - (ii) Show that if she continues on the same circular path, the reaction force exerted on her by the ground must act at an angle  $\theta$  to the vertical, where  $\tan \theta = \frac{v^2}{\sigma r}$ [6]



The diagram shows a uniform lamina ABCDE formed by removing a symmetrical triangular section from a rectangular sheet of metal measuring 30 cm by 25 cm. (i) Find the distance of the centre of mass of the lamina from ED. [3]

The lamina has mass *m*. A particle *P* is attached to the lamina at *B*.

The lamina is then suspended freely from A and hangs in equilibrium with AD vertical.

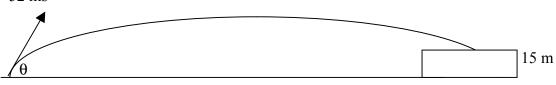
(ii) Find, in terms of *m*, the mass of *P*.

- A car, of mass 1100 kg, pulls a trailer of mass 550 kg along a straight horizontal road by means of 4. a rigid tow-bar. The car is accelerating at  $1.2 \text{ ms}^{-2}$  and the resistances to the motion of the car and trailer have magnitudes 500 N and 200 N respectively.
  - (i) Show that the driving force produced by the engine of the car is 2680 N. [3]
  - (ii) Find the tension in the tow-bar between the car and the trailer.
  - (iii) Find the rate, in kW, at which the car's engine is working when the car is moving with speed  $18 \text{ ms}^{-1}$ . [2]

When the car is moving at 18 ms<sup>-1</sup> it starts to climb a straight hill which is inclined at 6<sup>0</sup> to the horizontal. If the car's engine continues to work at the same rate and the resistances to motion remain the same as previously,

- (iv) find the acceleration of the car at the instant when it starts to climb the hill. [3]
- (v) Show that tension in the tow-bar remains unchanged.

5. Take  $g = 10 \text{ ms}^{-2}$  in this question. 52 ms<sup>-1</sup>



A golfer hits a ball from a point *T* at an angle  $\theta$  to the horizontal, where  $\sin \theta = \frac{5}{13}$ , giving it an initial speed of 52 ms<sup>-1</sup>. The ball lands on top of a mound, 15 m above the level of *T*, as shown.

(i) Show that the height, y m, of the ball above T at time t seconds after it was hit is given by

$$v = 20t - 5t^2.$$
 [3]

- (ii) Find the time for which the ball is in flight.
- (iii) Find the horizontal distance travelled by the ball.
- (iv) Show that, if the ball is x m horizontally from T at time t seconds, then

$$v = \frac{5}{12} x - \frac{5}{2304} x^2.$$
 [3]

- (v) Name a force that has been ignored in your mathematical model and state whether the answer to part (ii) would be larger or smaller if this force were taken into account. [2]
- 6. Two smooth spheres, *A* and *B*, of equal radius but of masses 3*m* and 4*m* respectively, are free to move in a straight horizontal groove. The coefficient of restitution between them is *e*.

A is projected with speed u to hit B, which is initially at rest.

- (i) Show that *B* begins to move with speed  $\frac{3}{7}u(1+e)$ . [5]
- (ii) Given that A is brought to rest by the collision, show that e = 0.75. [3]

Having been brought to rest, *A* is now set in motion again by being given an impulse of magnitude *kmu* Ns, where k > 2.25. *A* then collides again with *B*.

(iii) Show that the speed of A after this second impact is independent of k. [6]

## **MECHANICS 2 (C) TEST PAPER 5 : ANSWERS AND MARK SCHEME**

- 1. (i) Volume per second =  $12\pi(0.04)^2 = 0.0603 \text{ m}^3$  Mass= 60.3 kg M1 A1

   P.E. gained per sec. =  $60.3 \times g \times 25 = 14\ 778 \text{ J}$  A1

   K.E. gained per sec. =  $\frac{1}{2} \times 60.3 \times 12^2 = 4342 \text{ J}$  A1

   (ii) Power = total energy per second =  $19\ 120\ \text{Js}^{-1} = 19.1\ \text{kW}$  M1 A16
- 2. (i) Resultant force towards centre =  $mv^2/r$  B1
  - (ii) Forces acting on her are vertical weight = mg, reaction R at  $\theta$  to vertical. B1

PMT

[3]

[2]

	Contact with ground maintained, so $R \cos \theta = mg$	B1 B1
	Horizontally : $R \sin \theta = mv^2/r$ Divide : $\tan \theta = v^2/gr$	B1 M1 A1 7
3.	(i) $750(12.5) = 180(21) + 570 \overline{y}$ $\overline{y} = 9.82 \mathrm{cm}$	M1 A1 A1
	(ii) Must have centre of mass $12.5$ cm from ED	B1
	9.816m + 13M = 12.5(m + M) $0.5M = 2.684m$ $M = 5.37m$	M1 A1 M1 A1 8
4.	(i) $F - 700 = 1650 \text{ x } 1.2$ $F = 700 + 1980 = 2680 \text{ N}$	M1 A1 A1
	(ii) $F - 500 - T = 1100 \times 1.2$ $T = 2180 - 1320 = 860$ N	M1 A1
	(iii) $P = 2680 \times 18 = 48.2 \text{ kW}$	M1 A1
	(iv) $48240 = 18(700 + 1650g \sin 6^0 + 1650a)$ $a = 0.176 \text{ ms}^{-2}$	M1 A1 A1
	(v) For trailer, $T - 200 - 550g \sin 6^0 = 550(0.176)$ $T = 860$ N	M1 A1 12
5.	(i) $y = (52 \sin \theta)t - \frac{1}{2}gt^2 = 20t - 5t^2$	M1 A1 A1
	(ii) Lands when $y = 15$ $t^2 - 4t + 3 = 0$ $(t-1)(t-3) = 0$	M1 A1
	Ball is coming down, so $t = 3$	A1
	(iii) $x = (52 \cos \theta)t = 52 \times \frac{12}{13} t = 48t$ When $t = 3$ , $x = 144$ m	M1 A1
	(iv) $y = 20 \times \frac{x}{48} - 5 \times (\frac{x}{48})^2 = \frac{5}{12}x - \frac{5}{2304}x^2$	M1 M1 A1
	(v) Have ignored air resistance, which would make answer larger	B1 B1 13
6.	(i) Momentum : $3mu = 3mv_A + 4mv_B$ $3v_A + 4v_B = 3u$	B1
	Elasticity : $(v_B - v_A) / (-u) = -e$ $3v_B - 3v_A = 3eu$	M1 A1
	Add : $3u(1+e) = 7v_B$ $v_B = \frac{3}{7}u(1+e)$	M1 A1
	(ii) If $v_A = 0$ , $v_B = eu$ and $4v_B = 3u$ , so $e = 0.75$	M1 A1 A1
	(iii) Now <i>A</i> has speed $\frac{1}{3}ku$ $(v'_B - v'_A) / (0.75u - \frac{1}{3}ku) = -0.75$	M1 A1
	and $kmu+3mu = 3mv'_A + 4mv'_B$	B1
	$ku + 3u = 3v'_{A} + 4(v'_{A} - 0.75(0.75 - \frac{1}{3}k)u) = 7v'_{A} - 2.25u + ku$	M1 A1
	$v'_A = 0.75u$ , which is independent of k	A1 14

PMT